

Total No. of Printed Pages—8

5 SEM TDC STSH (CBCS) C 12 (N/O)

2024

(November)

STATISTICS

(Core)

Paper : C-12

(Statistical Computing Using C Programming)

*The figures in the margin indicate full marks
for the questions*

(New Course)

Full Marks : 55

Pass Marks : 22

Time : 3 hours

1. Choose the correct answer from the following alternatives : 1×6=6

(a) Who is the father of C language?

(i) Bjarne Stroustrup

(ii) James Gosling

(iii) Dennis Ritchie

(iv) W. A. Shewhart

(2)

- (b) How many keywords are there in C?
- (i) 0
 - (ii) 32
 - (iii) 48
 - (iv) 255
- (c) Which of the following will not return a value?
- (i) void
 - (ii) int
 - (iii) null
 - (iv) char
- (d) Nesting is allowed for which of the following statements?
- (i) if
 - (ii) if else
 - (iii) switch
 - (iv) All of the above
- (e) Where should the default values of parameter be specified?
- (i) Function call
 - (ii) Function definition
 - (iii) Function prototype
 - (iv) None of the above

(3)

- (f) Which of the following operations is allowed to be performed on a pointer variable?
- (i) $\text{ptr} + 1$
 - (ii) $\text{ptr} - 1$
 - (iii) $\text{ptr}++$ and $\text{ptr}--$
 - (iv) All of the above

2. Answer the following questions in brief :

$2 \times 6 = 12$

- (a) What is the difference between pre-increment and post-increment operations?
- (b) What are the disadvantages of do-while statement?
- (c) Explain the purpose of recursion function.
- (d) What is static memory allocation?
- (e) Differentiate between for loop and while loop.
- (f) What is pointer variable?

3. Answer any *two* of the following questions :

$8 \times 2 = 16$

- (a) Write a short history of C programming. What are the advantages and disadvantages of C programming?

$4 + 4 = 8$

(4)

- (b) What do you mean by identifiers? State the rules for naming identifiers. Give some examples of valid and invalid identifiers. $2+3+3=8$

- (c) Explain the basic data types supported by C language and discuss their features. $4+4=8$

4. (a) What is a loop? Compare the three loop control structures used in C with examples. $2+6=8$

Or

- (b) What is an array? Explain different types of array with syntax. $2+6=8$

5. (a) What is function prototype? Write a recursion function algorithm to find a factorial of a number. $2+5=7$

Or

- (b) Distinguish between library function and user-defined function. Explain in detail the storage classes available in C language with examples. $2+5=7$

6. (a) Distinguish between pointers and arrays. How to declare and initialize a pointer? Explain with examples. $3+3=6$

Or

- (b) What is dynamic memory allocation? Explain malloc() and calloc() functions. $3+3=6$

(5)

(Old Course)

Full Marks : 50

Pass Marks : 20

Time : 2 hours

1. Choose the correct answer from the following alternatives : $1 \times 5 = 5$

- (a) Who is the father of C language?

(i) Bjarne Stroustrup

(ii) James Gosling

(iii) Dennis Ritchie

(iv) W. A. Shewhart

- (b) How many keywords are there in C?

(i) 0

(ii) 32

(iii) 48

(iv) 255

- (c) Which of the following will not return a value?

(i) void

(ii) int

(iii) null

(iv) char

(6)

(d) Nesting is allowed for which of the following statements?

- (i) if
- (ii) if else
- (iii) switch
- (iv) All of the above

(e) Which of the following operations is allowed to be performed on a pointer variable?

- (i) $\text{ptr} + 1$
- (ii) $\text{ptr} - 1$
- (iii) $\text{ptr}++$ and $\text{ptr}--$
- (iv) All of the above

2. Answer the following questions in brief :

$2 \times 5 = 10$

- (a) What is the difference between pre-increment and post-increment operations?
- (b) What are the disadvantages of do-while statement?
- (c) Explain the purpose of recursion function.
- (d) What is static memory allocation?
- (e) What is pointer variable?

(7)

3. Answer any *two* of the following questions :

$7 \times 2 = 14$

(a) Write a short history of C programming. What are the advantages and disadvantages of C programming? $3+4=7$

(b) What do you mean by identifiers? State the rules for naming identifiers. Give some examples of valid and invalid identifiers. $1+3+3=7$

(c) Explain the basic data types supported by C language and discuss their features. $3+4=7$

4. (a) What is a loop? Compare the three loop control structures used in C with examples. $2+6=8$

Or

(b) What is an array? Explain different types of array with syntax. $2+6=8$

5. (a) What is function prototype? Write a recursion function algorithm to find a factorial of a number. $2+5=7$

Or

(b) Distinguish between library function and user-defined function. Explain in detail the storage classes available in C language with examples. $2+5=7$

6. (a) Distinguish between pointers and arrays. How to declare and initialize a pointer? Explain with examples. $3+3=6$

Or

- (b) What is dynamic memory allocation? Explain malloc() and calloc() functions. $3+3=6$

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5 SEM TDC STSH (CBCS) C 11 (N/O)

2024

(November)

STATISTICS

(Core)

Paper : C-11

(Stochastic Processes and Queuing Theory)

*The figures in the margin indicate full marks
for the questions*

(New Course)

Full Marks : 55

Pass Marks : 22

Time : 3 hours

1. Choose the correct answer from the following alternatives : 1×7=7

(a) Consider a Markov chain $\{X_n, n \geq 0\}$ with discrete state space. If the transition probabilities are independent of n , then the Markov chain is said to be

- (i) independent
- (ii) homogeneous
- (iii) reducible
- (iv) non-homogeneous

(2)

(b) If two states of a Markov chain are accessible from each other, then they are

- (i) communicating states
- (ii) transient states
- (iii) absorbing states
- (iv) periodic states

(c) Following is the t.p.m. for a Markov chain :

$$\begin{matrix} & \begin{matrix} 1 & 2 & 3 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \end{matrix} & \begin{bmatrix} 1-2a & 2a & 0 \\ a & 1-2a & a \\ 0 & 2a & 1-2a \end{bmatrix} \end{matrix}$$

Then the

- (i) value of a is any real number
 - (ii) value of a is any positive real number
 - (iii) value of a is less than 0.5
 - (iv) value of a is in $[0, 0.5]$
- (d) If $\{N(t)\}$ is a Poisson process, then the correlation coefficient between $N(t)$ and $N(t+s)$ is

(i) $\{t(t+s)\}^{3/2}$

(3)

(ii) $\frac{t}{t+s}$

(iii) $\left\{ \frac{(t+s)}{t} \right\}^{1/2}$

(iv) $\left\{ \frac{t}{(t+s)} \right\}^{1/2}$

(e) If $N_1(t)$ and $N_2(t)$ are two independent Poisson processes with parameters λ_1 and λ_2 respectively, then $N_1(t) - N_2(t)$ is

- (i) a Poisson process with rate $\lambda_1 + \lambda_2$
- (ii) a Poisson process with rate $\lambda_1 - \lambda_2$
- (iii) a Poisson process with rate $\frac{\lambda_1}{\lambda_2}$
- (iv) not a Poisson process

(f) $M/M/1$: model follows

- (i) geometric distribution
- (ii) exponential distribution
- (iii) Poisson distribution
- (iv) negative exponential distribution

(g) The term 'jockeying' in queuing theory refers to

- (i) not entering the long queue
- (ii) leaving the queue
- (iii) shifting from one queue to another parallel queue
- (iv) None of the above

2. Answer the following questions in brief : 2×6=12

- (a) Define a stochastic process with an example.
- (b) State Chapman-Kolmogorov theorem.
- (c) Define irreducible Markov chain and closed set.
- (d) Define transient and persistent states.
- (e) Prove that the interval between two successive occurrences of a Poisson process $\{N(t), t \geq 0\}$ having parameter λ has a negative exponential distribution with mean $\frac{1}{\lambda}$.

(f) What do the letters in the symbolic representation $(a/b/c):d/e$ of a queuing model represent?

3. (a) (i) Define bivariate probability generating function. Given the bivariate p.g.f. of (X, Y) as

$$P(s_1, s_2) = \exp[-a - b - c + as_1 + bs_2 + cs_1s_2]$$

Find the p.g.f. of $X + Y$ and identify the distribution. 1+1=2

- (ii) The r.v. X has logarithmic series distribution if

$$p_k = P(X = k) = \frac{Xq^k}{k}; \quad k = 1, 2, 3, \dots$$

$$X = -\frac{1}{\log p}; \quad 0 < q = 1 - p < 1$$

Find the p.g.f. of X . Also, find mean and variance. 3

Or

- (b) If $\{N(t)\}$ is a Poisson process and $s < t$, then prove that

$$P\{N(s) = k / N(t) = n\} = \binom{n}{k} \left(\frac{s}{t}\right)^k \left\{1 - \left(\frac{s}{t}\right)\right\}^{n-k} \quad 5$$

4. Answer any four questions from the following : 4×4=16

- (a) Interpret the Gambler's ruin problem as a Markov chain.

(6)

- (b) Consider the Markov chain with three states $S = \{1, 2, 3\}$, that has the following transition matrix :

$$P = \begin{bmatrix} \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ \frac{1}{3} & 0 & \frac{2}{3} \\ \frac{1}{2} & \frac{1}{2} & 0 \end{bmatrix}$$

- (i) Draw the transition diagram of the Markov chain.

- (ii) If $P(X_1 = 1) = P(X_2 = 2) = \frac{1}{4}$, then find $P(X_1 = 3, X_2 = 2, X_3 = 1)$. $2+2=4$

- (c) Let $\{X_n, n \geq 0\}$ is a Markov chain with t.p.m.

$$P = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{3} & \frac{2}{3} \end{bmatrix}$$

and initial distribution $P(X_0 = j) = \frac{1}{2}$;
 $j = 0, 1$

Compute—

- (i) $P(X_1 = 1)$;
(ii) $P(X_1 = 0)$;

(7)

- (iii) $P(X_2 = 1)$;

- (iv) $P(X_2 = 0)$.

$$1+1+1+1=4$$

- (d) Define ergodic state in Markov chain. Let $\{X_n, n \geq 0\}$ be a Markov chain having state space $s = \{1, 2, 3, 4\}$ and t.p.m.

$$P = \begin{bmatrix} \frac{1}{3} & \frac{2}{3} & 0 & 0 \\ 1 & 0 & 0 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

Show that state '1' is ergodic.

$$1+3=4$$

- (e) Define periodicity of a Markov chain. Show that the states of the Markov chain with t.p.m.

$$P = \begin{bmatrix} 0 & 1 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} \\ 0 & 1 & 0 \end{bmatrix}$$

are periodic and persistent non-null.

$$1+3=4$$

5. (a) (i) Show that the sum of two independent Poisson processes is a Poisson process.

$$2$$

(8)

- (ii) State the differential-difference equation of linear growth process and hence using the equation, show that $M'(t) = (\lambda - \mu)M(t)$, where

$$M(t) = \sum_{n=1}^{\infty} n \cdot P_n(t), \quad \lambda \text{ and } \mu \text{ are}$$

respectively the birth and death rates of the process $\{X_t\}$.

5

Or

- (b) Show that if the intervals between successive occurrences of an event E are independently distributed with a common exponential distribution with mean $\frac{1}{\lambda}$, then the event E forms a Poisson process with mean λt .

7

6. (a) Define a queuing system. Discuss the basic features which characterize a queuing system.
"Queue is a management of congestions."
Elucidate the statement.

4+4=8

Or

- (b) In case of $(M/M/1) : (N/FCFS)$ queuing model, derive the steady-state probability distribution and obtain the expression for—

- (i) expected number of customers in the system;
(ii) expected number of customers in the queue.

6+2=8

(9)

(Old Course)

Full Marks : 50

Pass Marks : 20

Time : 2 hours

1. Choose the correct answer from the following alternatives : 1×6=6

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2. Answer the following questions in brief :

2×5=10

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- (ii) If $P(X_1 = 1) = P(X_2 = 2) = \frac{1}{4}$, then find $P(X_1 = 3, X_2 = 2, X_3 = 1)$. 2+2=4

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and initial distribution $P(X_0 = j) = \frac{1}{2};$
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Compute—

- (i) $P(X_1 = 1);$
(ii) $P(X_1 = 0);$

(iii) $P(X_2 = 1)$;

(iv) $P(X_2 = 0)$.

$$1+1+1+1=4$$

- (d) Define ergodic state in Markov chain. Let $\{X_n, n \geq 0\}$ be a Markov chain having state space $S = \{1, 2, 3, 4\}$ and t.p.m.

$$P = \begin{bmatrix} \frac{1}{3} & \frac{2}{3} & 0 & 0 \\ 1 & 0 & 0 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

Show that state '1' is ergodic.

$$1+3=4$$

- (e) Define periodicity of a Markov chain. Show that the states of the Markov chain with t.p.m.

$$P = \begin{bmatrix} 0 & 1 & 0 \\ \frac{1}{2} & 0 & \frac{1}{2} \\ 0 & 1 & 0 \end{bmatrix}$$

are periodic and persistent non-null.

$$1+3=4$$

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$$M(t) = \sum_{n=1}^{\infty} n \cdot P_n(t), \quad \lambda \text{ and } \mu \text{ are}$$

respectively the birth and death rates of the process $\{X_t\}$.

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Or

- (b) Show that if the intervals between successive occurrences of an event E are independently distributed with a common exponential distribution with mean $\frac{1}{\lambda}$, then the event E forms a Poisson process with mean λt .

6

6. (a) Define a queuing system. Discuss the basic features which characterize a queuing system.

"Queue is a management of congestions." Elucidate the statement.

$$4+3=7$$

(Turn Over)

Or

(b) In case of $(M/M/1) : (N/FCFS)$ queuing model, derive the steady-state probability distribution and obtain the expression for—

(i) expected number of customers in the system;

(ii) expected number of customers in the queue. $5+2=7$

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